

# Deterministic Test Pattern Generation using Segmented LFSR

Lung-Jen Lee<sup>1</sup>, Wang-Dauh Tseng, Rung-Bin Lin, and You-An Chen  
*Department of Computer Science & Engineering*  
*Yuan Ze University, Chung-li, Taiwan, 32026, ROC*

<sup>1</sup>s959101@mail.yzu.edu.tw

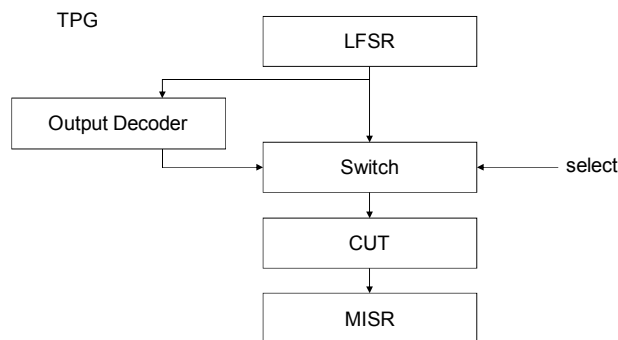
**Abstract** — A new test data generation technique combining traditional internal liner feedback shift register (LFSR) with a specific polynomial LFSR, is presented in this work. The specific polynomial LFSR (SP-LFSR) method explores the distributions of 0's and 1's in each column and logically gathers the columns with mostly 0's or 1's for generation. This approach reduces more test time than the traditional LFSR does. Most previous techniques reduce test application time at the expense of hardware overhead. In our new method, we analyze the test data and reorder the scan chain into two parts while feeding the test data. The hardware overhead is low, only some inverters and XOR gates are required.

**Index terms** — specific polynomial LFSR, test data generation

## 1. INTRODUCTION

Built-in self-test (BIST) is a technique that makes circuits test itself without using automatic test equipment (ATE). Linear feedback shift register (LFSR) are usually used as test pattern generator (TPGs) in low overhead BIST schemes. This is due to the fact that an LFSR can be built with little area overhead. By now, many BIST methods were developed [1]-[5], all of them trying to find some trade-off between these four mutually antipodal aspects: the fault coverage, test time, the area overhead and the BIST design time. Attainment of high fault coverage with sequences is the main objective of BIST techniques.

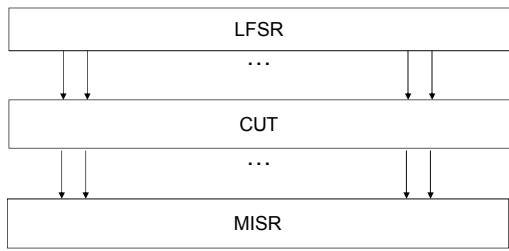
Achieving high fault coverage for CUTs that contain many random pattern resistant faults (RPRFs) only with pseudorandom patterns generated by an LFSR often requires unacceptably long test sequences and results in prohibitively long test time. A combination of a pseudo-random and deterministic BIST is being referred to as a mixed-



**Figure 1. Mixed-Mode Architecture**

mode BIST, the architecture shows in Figure 1. To support the mixed-mode testing, the test is divided into two disjoint phases, i.e., the pseudo-random phase and the deterministic phase. If test application time is long during pseudo-random phase, the output decoder is smaller. If test application time is short during pseudo-random phase, the output decoder is larger. Several techniques have been proposed to address this problem, e.g., reseedable and/or reconfigurable LFSRs in [6]-[8], bit-fixing and bit-flopping techniques in [2] and [4], and column-matching technique in [9] and [10].

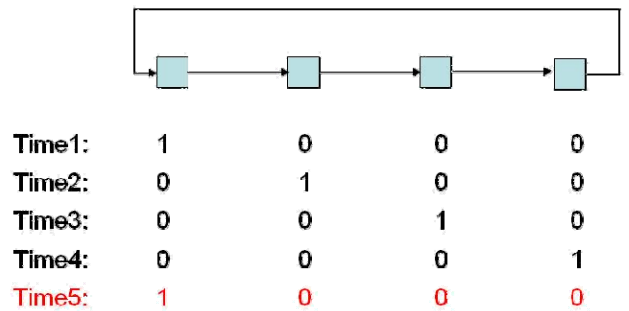
Scan-Based BIST can be simply classified into two types of test schemes: test-per-scan scheme and test-per-clock scheme. In test-per-clock BIST, a test pattern is applied and the test response is captured every clock cycle. Using test-per-clock scheme to generate test patterns needs fewer test patterns to reach the same fault coverage than the test-per-scan test scheme does. The architecture shows in Figure 2.



**Figure 2. Test-per-clock BIST architecture**

LFSRs can be simply classified into two types: internal LFSR and external LFSR. In internal LFSR, inputs of selected stages  $D_i$ , given by the feedback polynomial of the LFSR, are driven by two-input XOR gates whose inputs are driven by outputs of preceding LFSR stages  $D_{i-1}$  and the last stage  $D_n$ . Hence, unlike the external LFSR,  $Q_i(t)$  can be different from  $Q_{i-1}(t-1)$  in an internal LFSR if the input of  $D_i$  is connected to the output of  $D_{i-1}$  through a two-input XOR gate whose other input is driven by the output of the last stage ( $D_n$ ) of the LFSR. The architecture of internal LFSR is shown

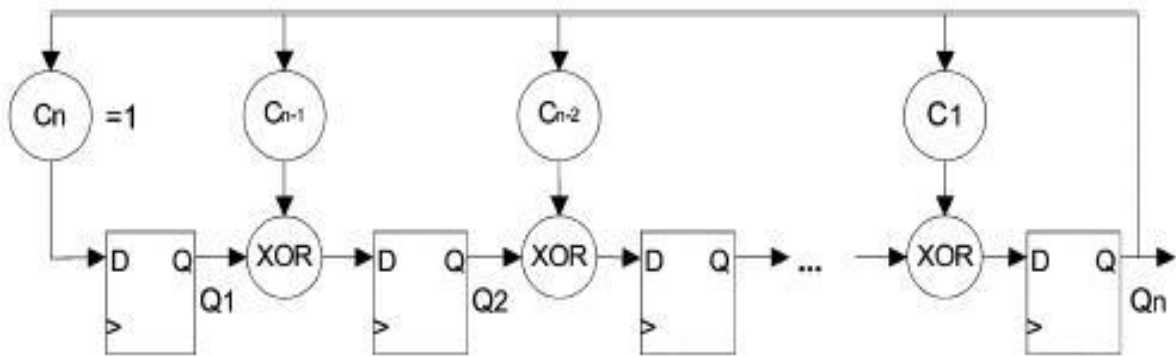
**Ring Counter**



**Figure 3. Ring counter architecture and test sequence**

in Figure 3. The ring counter is a special case of internal LFSR, the polynomial is  $X^N+1$ , as shown in Figure 4.

Figure 5 shows an architecture of mixed-mode BIST. First, LFSR is used to generate the test pattern to detect the easy-detect fault, and then bit-fixing technique is performed to fix random value to 0 or 1.



**Figure 4. Internal LFSR architecture**

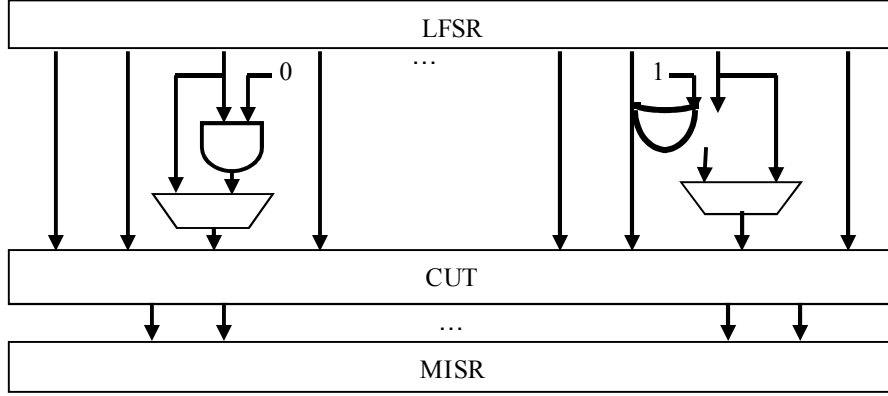


Figure 5. Mixed-mode architecture

Table 1. Test cube sets and detection probability

C	c6	c5	c4	c3	c2	c1	dp
P1	1	X	0	1	X	0	$1/2^4$
P2	X	1	0	0	0	X	$1/2^4$
P3	1	X	X	0	X	1	$1/2^3$
P4	0	1	X	0	0	1	$1/2^5$

Table 2. The new detection probability after bit-fixing is used

C	c6	c5	c4	c3	c2	c1	dp
P1	1	1	0	1	0	0	$1/2^3$
P2	X	1	0	0	0	X	$1/2$
P3	1	1	0	0	0	1	$1/2^3$
P4	0	1	0	0	0	1	$1/2^3$

Table 1 shows the test cube sets, input c2 is always assigned 0 or don't care bit (X) in Table 1. Therefore, input c2 is assigned to 0 in every test cycle. Similarly, input c4 is assigned to 0 and c5 is assigned to 1. In order to lock the value, the authors use an AND gate to lock value to 0 and use an OR gate to lock value to 1.

The dp is detection probability, and it is simply given by  $1/2^{\text{the number of care bits}}$ . If input can be fixed to 0(1) (with underline in Table 2) without making any fault undetectable, the dp can be increased as shown in Table 2.

## 2. PROPOSED METHOD

We proposed a methodology to reduce test application time during the test mode. Several techniques have been proposed to address this problem. The mixed-mode BIST is used to detect

hard-to-detect fault which is undetectable after RTPG patterns are applied. If test application time is long during pseudo-random phase, the output decoder is smaller. If test application time is short during pseudo-random phase, the output decoder is larger. The proposed method is to reduce application time that test patterns generated by the pseudo-random phase detect easy-to-detect faults. The proposed test scheme uses traditional LFSR and SP-LFSR to generate test patterns to detect easy-to-detect faults, the architecture as shown in Figure 6. The characteristic of internal LFSR is that scan cells would be partitioned according to the distribution of number 0 and 1. The ratio of don't care-bit in the test patterns is very important when the scan chain is partitioned. If the don't care-bit ratio is low, it is hard to find columns that generated by SP-LFSR.

Let us consider an RTPG that uses an internal LFSR where initial value  $D_1D_2...D_N$  is  $100...0$ . The  $D_n$  is 0 from the first cycle to the (n-1)th cycle, so the input of stage  $D_i$ , where  $i = 2, 3, \dots, n$ , is directly driven by the output of the preceding LFSR stage  $D_{i-1}$  and the  $D_1$  is driven by the  $D_n$  during the (n-1) cycle. As show in Figure 7(a), it is the sequence that test patterns generated by the RTPG when LFSR size is 4 and seed is 1000. Internal LFSR has a special characteristic that there is only single 1 from P1 to P4 in the test patterns. Another characteristic of LFSR is to generate the shortest test pattern sequence when polynomial is  $X^n+1$  and the seed is  $100...0$ , we call the architecture as ring counter. Fig 7.(b) show the result when polynomial is  $X^4+1$  and seed is 1000. The rule is true when  $n > 1$ .

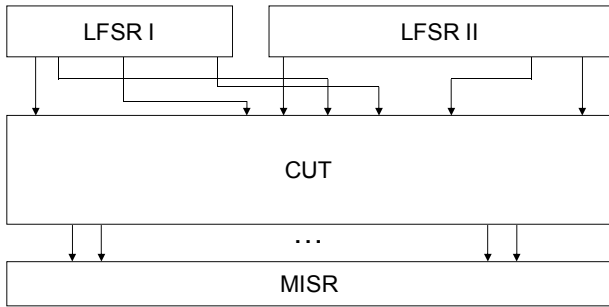


Figure 6. Proposed Architecture

P1 : 1 0 0 0
P2 : 0 1 0 0
P3 : 0 0 1 0
P4 : 0 0 0 1
P5 : ...
Test patterns

P1 : 1 0 0 0
P2 : 0 1 0 0
P3 : 0 0 1 0
P4 : 0 0 0 1
P5 : 1 0 0 0
Test patterns

(a)

(b)

Figure 7(a). LFSR size is 4 and seed is 1000. (b) Polynomial is  $X^4+X^3+X^2+X+1$  and seed 1000

Table 3. Test cubes

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10
P1	1	0	X	1	1	X	X	X	1	X
P2	0	0	X	1	0	0	0	1	X	X
P3	X	0	X	1	1	X	X	X	0	X
P4	X	0	0	0	1	X	0	1	0	X
P5	X	0	X	X	X	1	1	1	X	1
P6	1	X	0	1	X	1	1	X	X	X
P7	X	0	X	X	X	0	1	X	X	0
P8	1	0	X	0	X	X	X	X	X	X
P9	X	0	X	X	1	X	X	0	X	1
P10	X	1	0	1	1	X	1	0	X	X

There are a lot of don't-care bits in test patterns, if we don't merge the test patterns. We try to collect columns that can be generated by SP-LFSR, and then use traditional LFSR and SP-LFSR to generate each test pattern. For example as show in Table 3, there are 10 test cubes and each test cube has 10 bits.

Firstly, we count the number of 0 and 1 in each column (Table 4). If the number of 1's is more than

Table 4. The number of 1 and 0 in each column.

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10
1 bits	3	1	0	5	5	2	4	3	1	2
0 bits	1	8	3	2	1	2	2	2	2	1
Inver	0	X	X	0	0	X	0	0	X	0

Table 5. Test cubes after invert.

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10
P1	0	0	X	0	0	X	X	X	1	X
P2	1	0	X	0	1	0	1	0	X	X
P3	X	0	X	0	0	X	X	X	0	X
P4	X	0	0	1	0	X	1	0	0	X
P5	X	0	X	X	X	1	0	0	X	0
P6	0	X	0	0	X	1	0	X	X	X
P7	X	0	X	X	X	0	0	X	X	1
P8	0	0	X	1	X	X	X	X	X	X
P9	X	0	X	X	0	X	X	1	X	0
P10	X	1	0	0	0	X	0	1	X	X

Table 6. The columns generated by SP-LFSR

	C1	C2	C3	C4	C6	C9	C10
P1	0	0	X	0	X	1	X
P2	1	0	X	0	0	X	X
P3	X	0	X	0	X	0	X
P4	X	0	0	1	X	0	X
P5	X	0	X	X	1	X	0
P6	0	X	0	0	1	X	X
P7	X	0	X	X	0	X	1
P8	0	0	X	1	X	X	X
P9	X	0	X	X	X	X	0
P10	X	1	0	0	X	X	X

0's, the column would be inverted to increase the number of columns that can be generated by SP-LFSR. Table 5 shows the test patterns after invert.

Secondly, we collect columns that can be generated by SP-LFSR. We reorder the columns according to the number of 1's in each column. In this case, the sequence is C3, C1, C2, C5, C9, C10, C4, C6, C7, C8. We select C3 at first and find no any row conflict with C, so, we add the C3 to S. Because the C3 has no 1 in any row, we update  $C = \{0,0,0,0,0,0,0,0,0,0\}$ . After that we select C1, and find no any row conflict with C. So, we add C1 to S, and update  $C = \{0,1,0,0,0,0,0,0,0,0\}$ . And then, we add S2 to S, and update  $C = \{0,1,0,0,0,0,0,0,0,1\}$ .

When C5 is selected, we find the second row is 1 which is conflict with C, so, we don't add C5 to S. Finally, we find the set  $S = \{C1, C2, C3, C4, C6, C9, C10\}$ . As show in Table 6,  $C = \{1,1,0,1,1,1,1,0,1\}$ .

The final result is shown in Fig 8. The tradition method uses 121 cycles to detect all cubes, but our method only uses 44 cycles.

The test application time is affected by the number of 1 in C. The reason for the longer test application time is illustrated by Table 7. In Case I, the test cube is detected when the test pattern is 0010000000. In Case II, the test cube is detected when test patterns are 0100000000, 0001000000, 0000100000, 0000000100 and 0000000001. The authors remove columns which the number of 1 is more than the number of total test patterns  $\times 5\%$ , as shown in Figure 9. Another, the authors remove columns until the total number of 1 less than the number of total test patterns  $\times 25\%$ , as shown in Figure 10.

A special polynomial LFSR used to advance the detection probability, the polynomial is  $X^N + X^{N/2} + 1$ ,

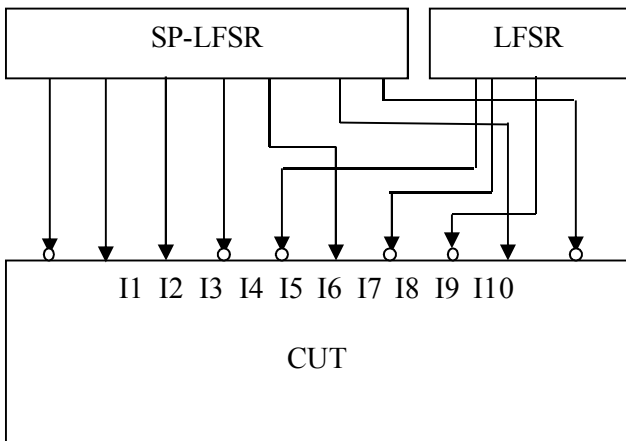


Figure 8. The final link

Table 7. The test cubes and the corresponding detection probability by Ring Counter.

	Test cubes	detection probability
Case I	0 X 1 X X 0 0 X 0 X	1/10
Case II	0 X 0 X X 0 0 X 0 X	5 /10

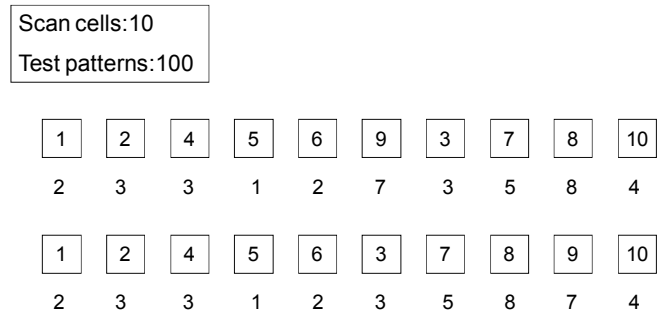


Figure 9. Removing the columns which the number of 1's is more than the number of total test patterns  $\times 5\%$

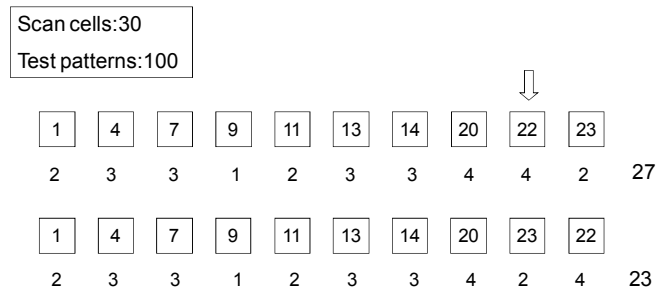


Figure 10. Removing columns until the total number of 1's is less than the number of total test patterns  $\times 25\%$

as shown in Figure 11. Figure 10 shows the test sequence increases from N to  $3/2N$ . The hardware overhead is an XOR gate. The Max transition increases from 2 to 4. The detection probability increases as shown in Figure 12.

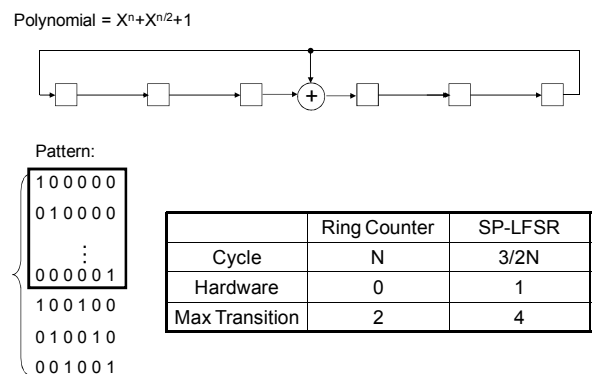


Figure 11. The architecture of SP-LFSR

	Test cube	detection probability
Case I	0 X 1 X X 0 0 X 0 X	2/15
Case II	0 X 0 X X 0 0 X 0 X	6/15

Case I:	000000001	000010001	Case II:	000000001	000010001
	000000010	000100010		000000010	000100010
	000000100	001000100		000000100	001000100
	000001000	010001000		000001000	010001000
	000010000	100010000		000010000	100010000
	000100000			000100000	
	001000000			001000000	
	001000000			001000000	
	010000000			010000000	
	010000000			010000000	
	100000000			100000000	

**Figure 12. The detection probability using SP-LFSR**

### 3. EXPERIMENTAL RESULTS

The experiments presented in the paper are focused on reducing the test application time and low hardware overhead. This work is implemented by C++ language and is performed on ISCAS'89 benchmarks. Table 8 shows the characteristics of the benchmark. The table shows the number of scan cells, test patterns in each circuit. It also shows the percentage of don't care bits in each circuit.

The experiments were designed to detect the easy-to-detect faults. In order to compare the test application time applied by ring counter, SP-LFSR and Traditional LFSR test sequence, the same fault coverage is set for each circuit.

Table 9 compares the application time applied by test patterns generated by ring counter with those generated by Traditional LFSR. The column labeled Total patterns shows the number of total test patterns for each benchmark circuit and column labeled Hit patterns shows the number of test patterns detected to each benchmark circuit. The labeled FC shows fault coverage achieved by test sequence. In order to compare application time applied candidly, the authors set the same seed (10...00) and polynomial of Traditional LFSR ( $X^n+X+1$ ). The column labeled Traditional LFSR

shows the length of the test sequence that Tradition LFSR applied to each circuit and column ring counter shows the length of the test sequence that ring counter applied to each circuit. The column labeled Test time reduction shows the improvement in test application time using ring counter. The column labeled XOR gates shows the number of total XOR gates used to each benchmark circuit. Table 10 compares the application time applied by test patterns generated by SP-LFSR with those generated by Traditional LFSR. Table 11 compares the fault coverage achieved by test pattern generated by ring counter with those generated by Traditional. The column labeled Time shows the test application time applied to each circuit. The column labeled Traditional LFSR FC(%) shows fault coverage achieved using

**Table 8. The characteristics of the benchmarks**

Circuit	# of Scan cells	# of test patterns	Don't care bit percent
S526	24	554	76%
S820	23	850	66%
S1238	31	1284	71%
S1269	54	1341	83%
S1423	91	1488	92%
S1512	86	407	93%
S9234	247	6480	95%

**Table 9. Test length comparison between Ring Counter with Traditional LFSR**

Circuit	#Total patterns	#Hit patterns	#FC	Traditional LFSR	Ring Counter	Improve (%)	#XOR gates
S526	554	553	99.8%	23559	19548	17.03	1
S820	850	850	100%	92326	27292	70.44	1
S1238	1284	1164	90.6%	27067	7152	73.58	1
S1269	1341	1274	95.0	542119	18556	96.58	1
S1423	1488	1453	97.6%	476030	107230	77.47	1
S1512	407	375	92.1%	16386	2293	86.01	1
S9234	6480	5798	89.4%	3497280	360317	89.70	1
Average						72.97	

**Table 10. Test length comparison between SP-LFSR with Traditional LFSR**

Circuit	#Total patterns	#Hit patterns	#FC (%)	Tradition Method	SP-LFSR	Improve (%)	#XOR gates
S526	554	553	99.8	23559	16273	30.93	2
S820	850	850	100	92326	15340	83.38	2
S1238	1284	1164	90.6	27067	7710	71.51	2
S1269	1341	1274	95.0	542119	18098	96.66	2
S1423	1488	1453	97.6	476030	103147	78.33	2
S1512	407	375	92.1	16386	2056	87.45	2
S9234	6480	5798	89.4	3497280	481511	86.23	2
Average						76.36	

Traditional LFSR generator the test pattern by test sequence. The column labeled Ring Counter FC(%) shows fault coverage achieved using ring counter generator the test pattern by test sequence. The column labeled Improve shows the improvement in fault coverage using ring counter. Table 12 compares the fault coverage achieved by test pattern generated by SP-LFSR with those generated by Traditional.

**Table 11. Fault coverage comparison between Ring Counter with Traditional LFSR**

Circuit	Time	Traditional LFSR (%)	Ring Counter (%)	Improve (%)
S526	23559	99.8	99.8	0
S820	92326	100	100	0
S1238	27067	90.6	98.13	7.48
S1269	542119	95.0	97.99	2.99
S1423	476030	97.6	98.86	1.21
S1512	16386	92.1	95.58	3.44
S9234	3497280	89.4	94.85	5.37

#### 4. CONCLUSIONS

In this paper, we propose a new architecture of test generation to reduce the test application time without sacrificing fault coverage. The scan chain is partitioned into two parts according to the distribution in number of 1's and 0's. Test data in the two parts are generated by the SP-LFSR and the traditional LFSR respectively. Results show the test application time can be reduced efficiently compared with traditional LFSR architecture.

**Table 12. Fault coverage comparison between SP-LFSR with Traditional LFSR**

Circuit	Time	Traditional LFSR (%)	SP-LFSR (%)	Improve (%)
S526	23559	99.8	99.8	0
S820	92326	100	100	0
S1238	27067	90.6	99.07	8.42
S1269	542119	95.0	98.14	3.14
S1423	476030	97.6	98.72	1.07
S1512	16386	92.1	95.82	3.68
S9234	3497280	89.4	94.24	4.76

## REFERENCES

- [1] V.K. Agrawal, C.R. Kime and K.K. Saluja. A tutorial on BIST, part 1: Principles, IEEE Design & Test of Computers, vol.10, No.1 March 1993, pp. 73-83, part 2:Applications, No.2 June 1993, pp. 69-77.
- [2] H.J. Wunderlich and G. Keifer. Bit-Flipping BIST, Proc. ACM/IEEE International Conference on CAD-96 (ICCAD96), San Jose, California, November 1996, pp. 337-343.
- [3] N.A. Toubia and E.J. McCluskey. Altering a Pseudo-Random Bit Sequence for Scan-Based BISR, Proc. of ITC'96, PP. 167-175.
- [4] N.A. Toubia and E.J. McCluskey. Bit-Fixing in Pseudorandom Sequences for Scan BIST, IEEE TCAD, Vol. 20, No. 4, April 2001. pp 545-555.
- [5] M. Chatterjee and D.K. Pradhan. A BIST Pattern Generator Design for Near-Perfect Fault Coverage, IEEE Transactions on Computers, vol. 52, no. 12, December 2003, pp. 1543-1558.
- [6] S. Hellebrand, J. Rajski, S. Tarnick, S. Venkataraman, and B.Courtois, "Built-In test for circuits with scan base on reseeding of multiple-polynomial linear feedback shift registers," IEEE Trans. Comput., vol. 44, no.2, pp. 223-233, Feb. 1995.
- [7] N. Zacharia, J. Rajski, and J. Tyszer, "Decompression of test data using variable-length seed LFSRs," in Proc. IEEE 13th VLSI Test Symp., 1995, pp. 426-433.
- [8] S. Hellebrand, J. Rajski, S. Tarnick, "Generation of vector patterns through reseeding of multiple-polynomial linear feedback shift registers," in Proc. IEEE Int. Test Conf., 1992, pp. 120-129.
- [9] Fišer, P., Hlavička, J., Kubátová, H.: "Column-Matching BIST Exploiting Test Don't-Cares", Proc. 8th IEEE European Test Workshop, Maastricht, 2003, pp. 215-216
- [10] Fišer, P., Kubátová, H.: "An Efficient Mixed-Mode BIST Technique", Proc. 7th IEEE Design and Diagnostics of Electronic Circuits and Systems Workshop 2004, Tatranská Lomnica, SK, 18.-21.4.2004, pp. 227-230
- [11] Seongmoon Wang, Sandeep K. Gupta, "LT-RTPG: A New Test-Per-Scan BIST TPG for Low Switching Activity," IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, vol. 25, no. 8, August 2006